

[<c219ec5f>] security\_sk\_free+0xf/0x20
[<c2451efb>] \_\_sk\_free+0x9b/0x120
[<c25ae7c1>] ? \_raw\_spin\_unlock\_irqres
[<c2451ffd>] sk\_free+0x1d/0x30
[<c24f1024>] unix\_release\_sock+0x174/0

#### Designing, Modeling, and Optimizing Transactional Data Structures

PhD Dissertation Defense

#### **Ahmed Hassan**

Electrical and Computer Engineering Department
Virginia Tech
September 1, 2015

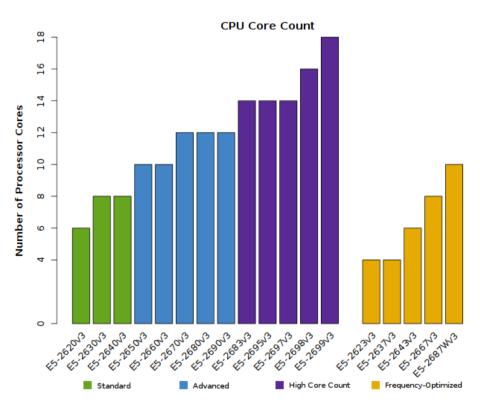




#### State of the Art

- Multi-core architectures.
- Synchronization
  - Critical sections.
  - Using locks.

- Efficient synchronization:
  - Cache coherence protocols.
  - Atomic instructions
    (e.g. CAS operations).



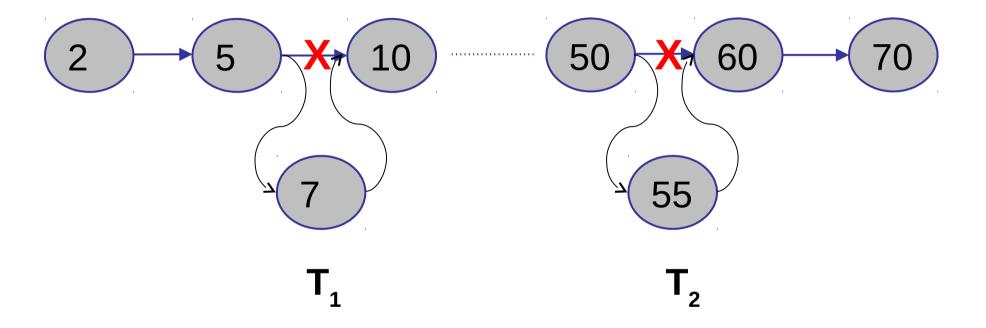
From www.microway.com

# Concurrent Data Structures

#### **Example: Linked List**



#### **Example: Linked List**



#### **Synchronization in Concurrent Data Structures**

- Coarse-grained locking
  - Easy to implement, good for low number of small threads .
  - But minimizes concurrency.
- Fine-grained locking
  - Allows more concurrency.
  - But error prone.
- Non-Blocking Designs
  - Lock-free, obstruction-free, wait-free, ...
  - Progress guarantees But more complex designs.

#### **Transactional Memory**

 Use an underlying TM framework to guarantee consistency, atomicity, and isolation.

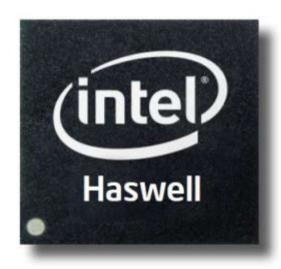
```
Thread 1

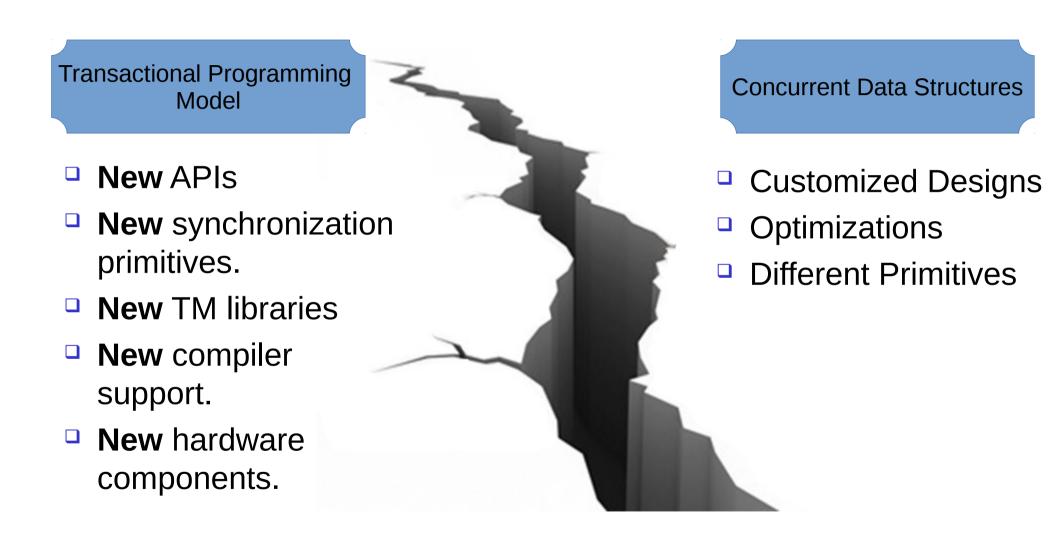
@Atomic
foo1()
{
    seqList.add(5)
}
```

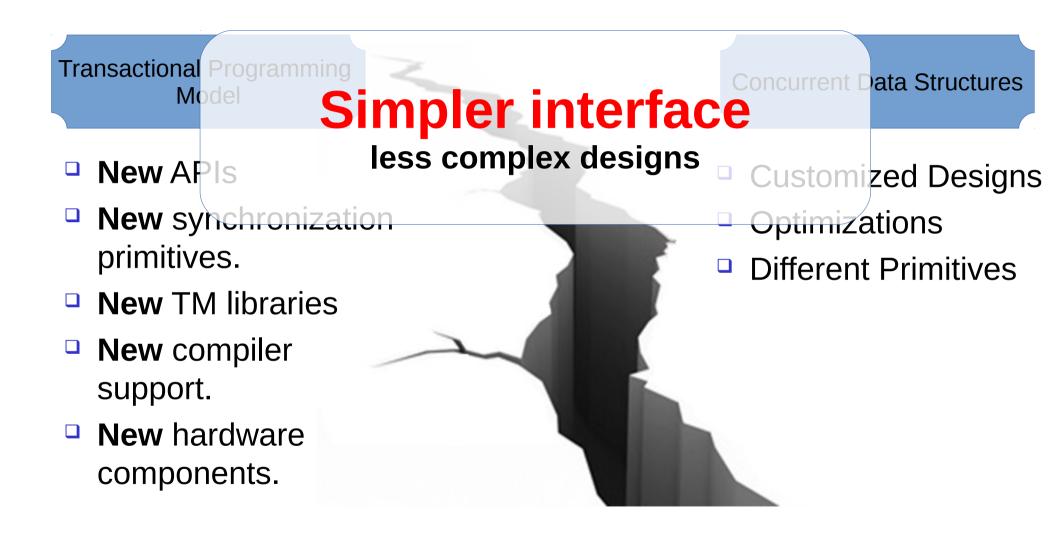
- Programmable (like coarse-grained locking).
- Allows concurrency (like fine-grained locking).

#### **Transactional Memory Gains Traction!!**

- Intel Haswell's TSX Extensions.
- IBM Power8.
- STM support in C++ and GCC.







Transactional Programming Concurrent Data Structures Model Simpler interface less complex designs **New** APIs **Customized Designs New** synchronization **Intimizations** primitives. ifferent Primitives New TM librariestomic transaction New compiler instead of atomic operations support, New hardware components.

support.

Transactional Programming
Model Simpler interface

less complex designs

Customized Designs

New Synchronization
primitives.

New TM librariestomic transaction
New compiler instead of atomic operations

New hardware components.
 Hardware Support

possible performance improvement

#### **Our Goal**

**From Concurrent to Transactional Data Structures** 

#### **Challenges**

- Composability.
- Integration with generic transactions.
- Modeling.



#### **Composability**

```
Shared data: concurrentList
atomicFoo()
{
     concurrentList.add(x);
}
```



```
Shared data: concurrentList

atomicFoo()
{
      concurrentList.add(x);
      concurrentList.add(y);
}
```



```
Shared data: concurrentList1
Shared data: concurrentList2

atomicFoo()
{
        concurrentList1.remove(x);
        concurrentList2.add(x);
}
```

#### Composability

```
Shared data: concurrentList

atomicFoo()
{

concurrentList.add(x);
```

### Modify the design of concurrentList? More complex designs

```
Shared data: concurrentList
atomicFoo()
{
      concurrentList.add(x);
      concurrentList.add(y);
}
```

```
Shared data: concurrentList1
Shared data: concurrentList2

atomicFoo()
{
        concurrentList1.remove(x);
        concurrentList2.add(x);
}
```

#### Composability

```
Shared data: concurrentList

atomicFoo()
{
    concurrentList.add(x);
```

## Modify the design of concurrentList? More complex designs

```
Shared data: concurrentList

Transactional

atomicFoo()
{ Lose optimizations of concurrentList.

concurrentList.add(x);

concurrentList.add(y);
}

concurrentList.add(y);
}

Shared data: concurrentList1

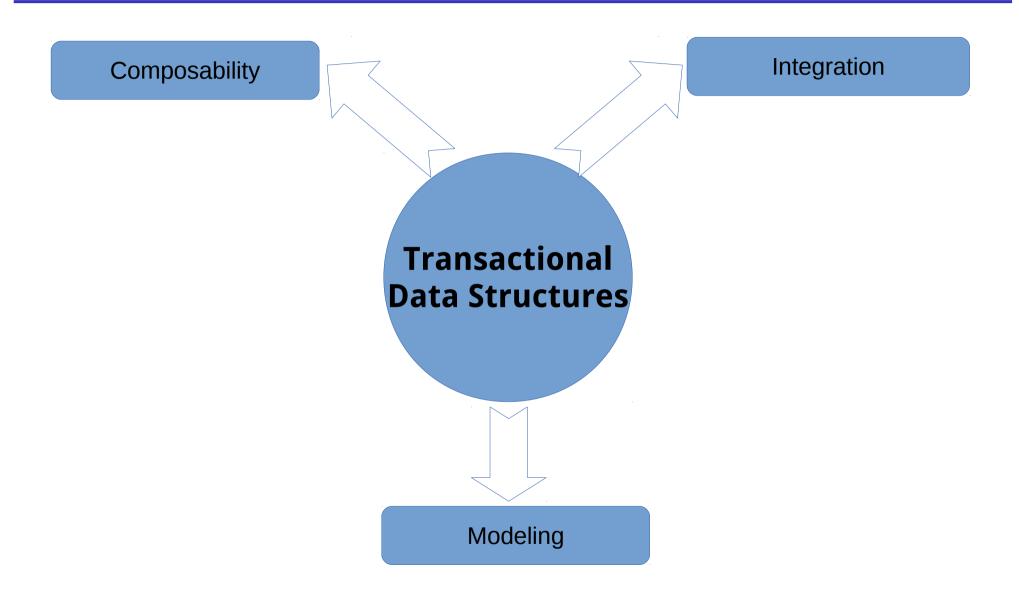
Memoryo?currentList2

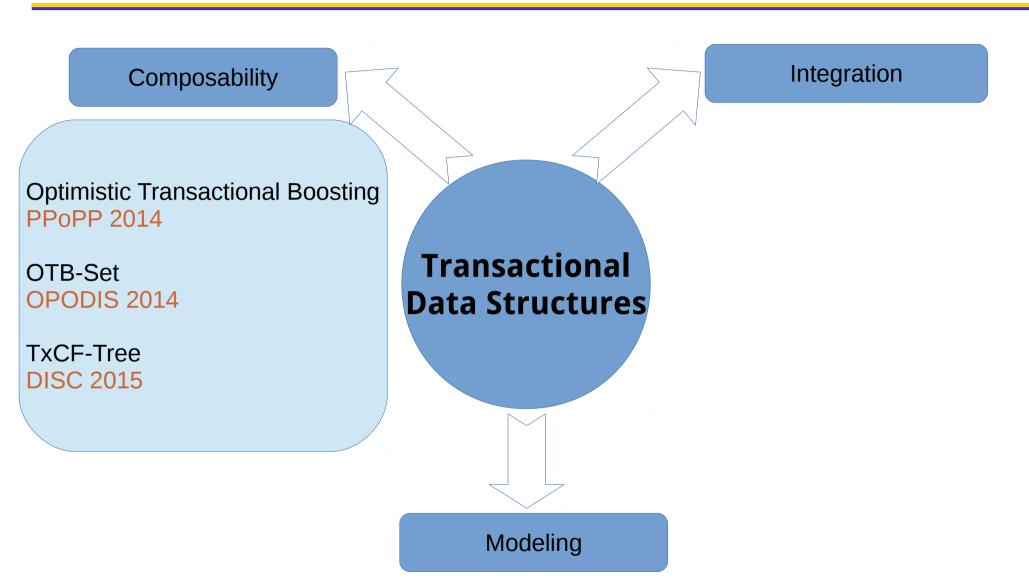
{ concurrentList1.remove(x);
 concurrentList2.add(x);
}
```

#### Integration

#### **Modeling**

- Different Designs and Implementations
  - Different ad-hoc approaches for proving correctness.
- Is there a unified model for concurrent data structures?
  - General enough
  - Easy to use
  - Includes composability and integration





Composability

Optimistic Transactional Boosting PPoPP 2014

OTB-Set OPODIS 2014

TxCF-Tree DISC 2015

Transactional Data Structures

Integration

Integration with STM TRANSACT 2014

Integration with HTM Under submission

Remote Transaction Commit IEEE TC 2015

Remote Invalidation IPDPS 2014

Modeling

#### Composability

Optimistic Transactional Boosting PPoPP 2014

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Transactional Data Structures

#### Integration

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SWC and C-SWC Models WTTM 2015, under submission

#### Composability

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Transactional Data Structures

Integration

Integration with STM

Integration with HTM

Under submission

Remote Transaction Commit

Remote Invalidation

MP/DP/S/2014

Modeling

SWC and C-SWC Models WTTM 2015, under submission

# Past and Related Work

#### **Past and Related Work**

- Composability and Integration
  - Transactional Memory.
  - Transactional Boosting.
- Modeling
  - SWMR Model

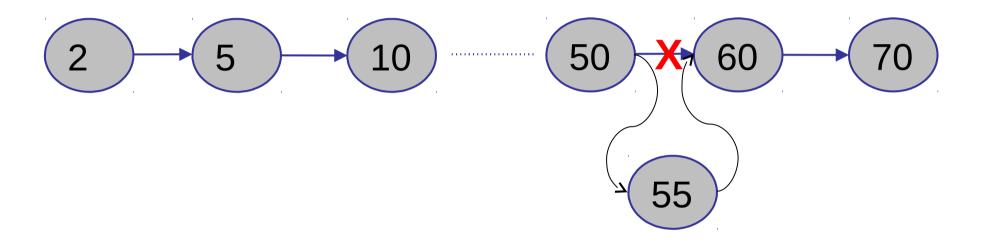
#### **Past and Related Work**

- Composability and Integration
  - Transactional Memory.
  - Transactional Boosting.
- Modeling
  - SWMR Model

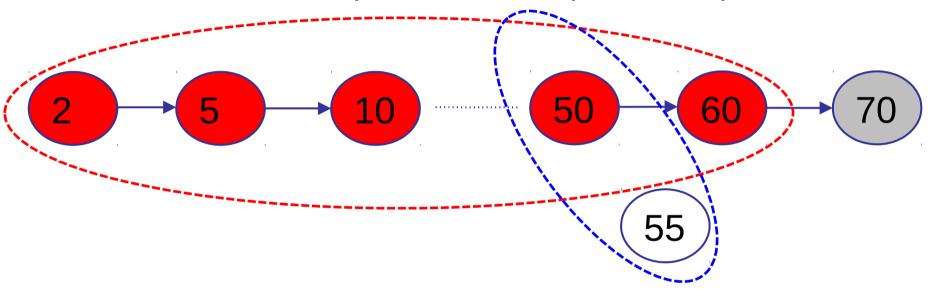
#### **Transactional Memory**

- Software Transactional Memory (STM)
  - SW meta-data (e.g. read-sets and write-sets) on the current HW.
- Hardware Transactional Memory (HTM)
  - New HW (modify cache coherency protocols).
- Hybrid Transactional Memory (Hybrid TM)
  - HTM transactions fall-back to STM

Example: Linked list (Insert "55")

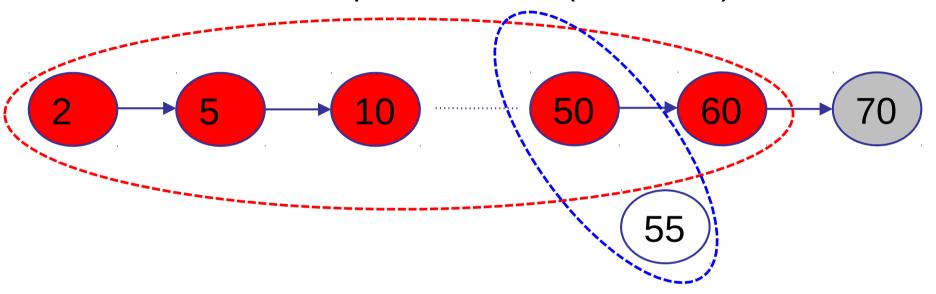


Example: Linked list (Insert "55")



All "red" nodes are in the read-set "50" and "55" are in the write-set

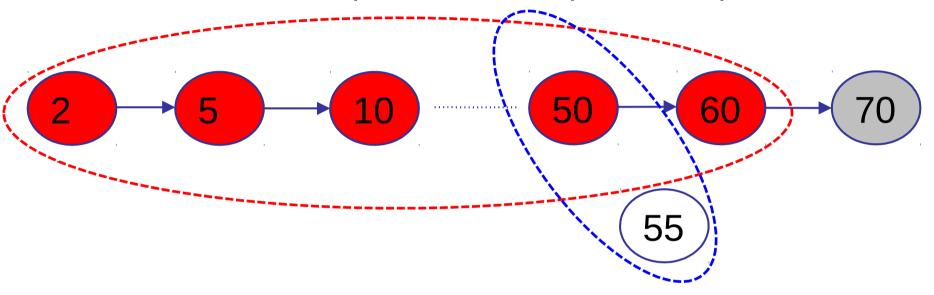
Example: Linked list (Insert "55")



All "red" nodes are in the read-set "50" and "55" are in the write-set

What if a concurrent transaction deletes "5"??

Example: Linked list (Insert "55")



All "red" nodes are in the read-set "50" and "55" are in the write-set

What if a concurrent transaction deletes "5"??

**False Conflict** 

#### **Transactional Boosting**

- Convert highly concurrent data structures to be transactional.
- Composable (like STM)
- And efficient (like lazy/lock-free linked-list)

Acquire Semantic Locks

Update Semantic undo-log

Call
Concurrent
Operation
(As Black Box)

Release Semantic Locks

(If Abort, roll back undo-log)

#### **Transactional Boosting**

- Convert highly concurrent data structures to be transactional.
- Composable (like STM)
- And efficient (like lazy/lock-free linked-list)
- Issues:
  - Eager locking.
  - Inverse operations.
  - Black-box concurrent data structure.
  - No Straightforward Integration

Acquire Semantic Locks

Update Semantic undo-log

Call
Concurrent
Operation
(As Black Box)

Release Semantic Locks

(If Abort, roll back undo-log)

#### **Optimistic Transactional Boosting**

#### **Past Solutions**

TM-BEGIN

Sequential Tree

TM-END

Acquire Semantic Locks

**Concurrent Tree** 

Release Semantic Locks

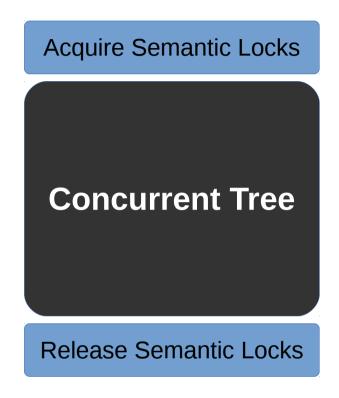
Transactional Memory

**Transactional Boosting** 

#### **Past Solutions**

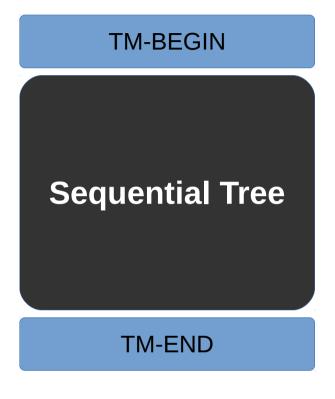


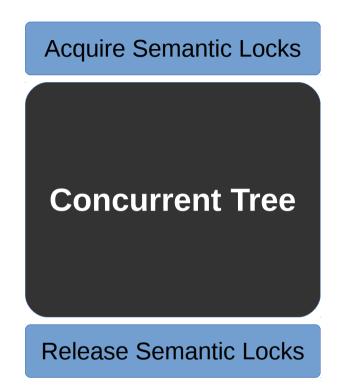
Transactional Memory



**Transactional Boosting** 

#### **Past Solutions**





Transactional Memory

**Transactional Boosting** 

General, BUT not optimized.

• G1: Split operation

**Concurrent Operation (add, remove, contains, ...)** 

• G1: Split operation

**Concurrent Operation (add, remove, contains, ...)** 



Traversal (long - unmonitored)

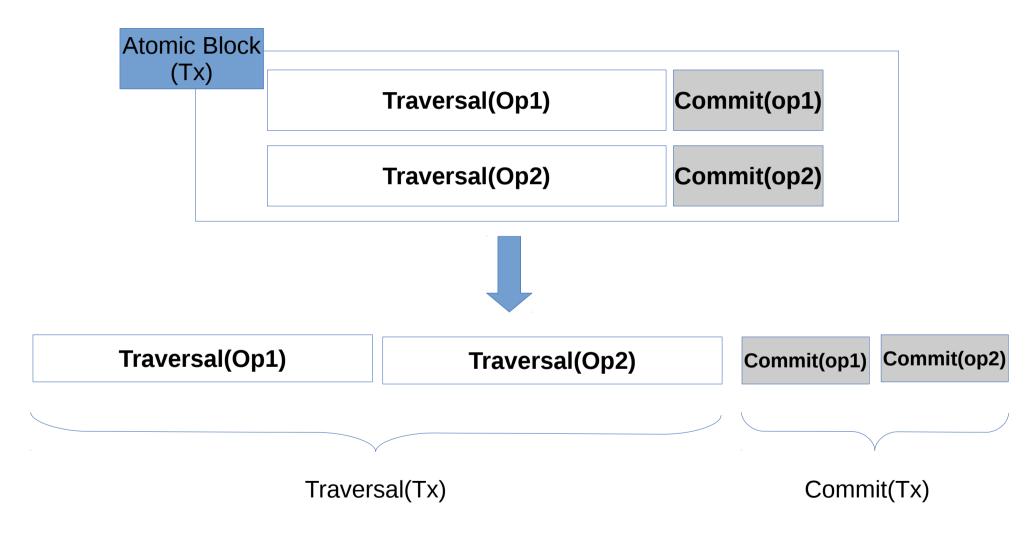
Commit (short - monitored)

• G2: Compose phases.

• G2: Compose phases



• G2: Compose phases



• G3: Optimize

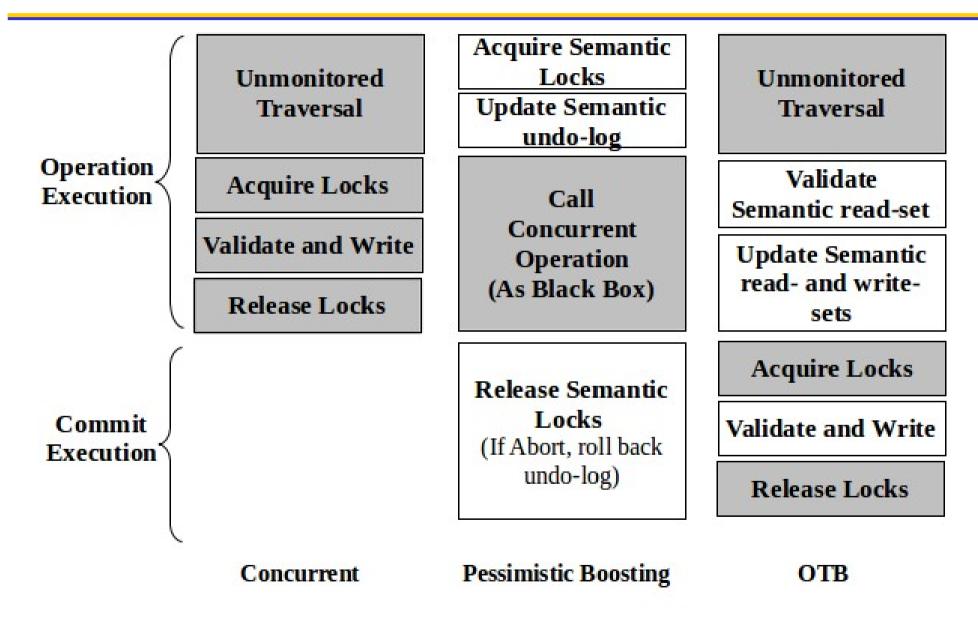
- G3: Optimize
  - Specific to each data structure.

- Our Contribution:
  - Linked-list-based Set.
  - Skip-list-based Set.
  - Skip-list-based Priority Queue.
  - Balanced Tree

- G3: Optimize
  - Specific to each data structure.

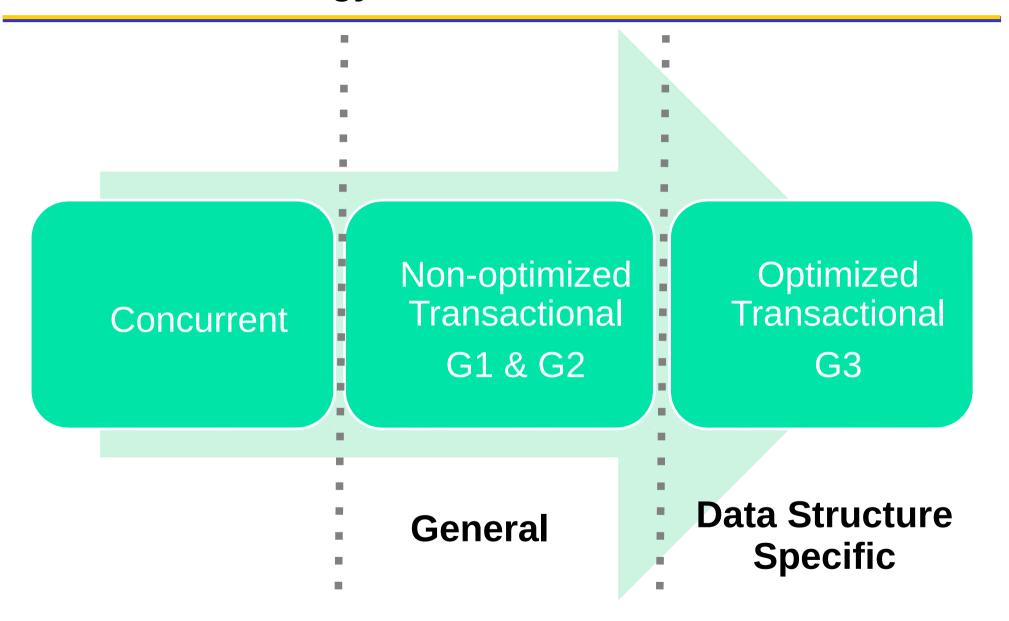
- Our Contribution:
  - Linked-list-based Set.
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  - Balanced Tree

# **Lazy Vs Boosting Vs Optimistic Boosting**



**Example Bootsing "lazy" concurrent linked list** 

# **OTB Methodology**



Lazy Linked list (Insert "55")

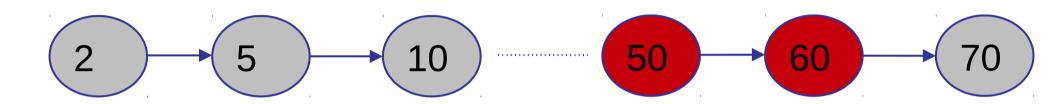


Lazy Linked list (Insert "55")



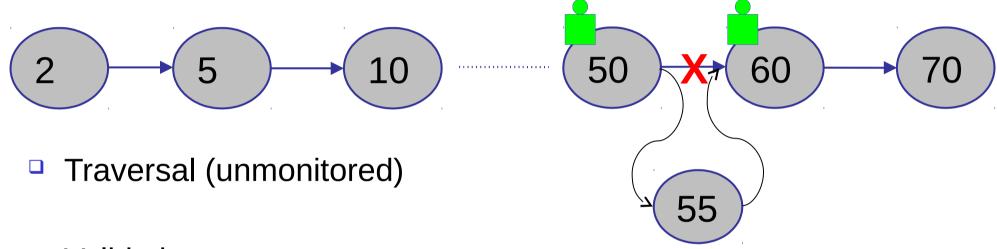
Traversal (unmonitored)

Lazy Linked list (Insert "55")



- Traversal (unmonitored)
- Validation

Lazy Linked list (Insert "55")



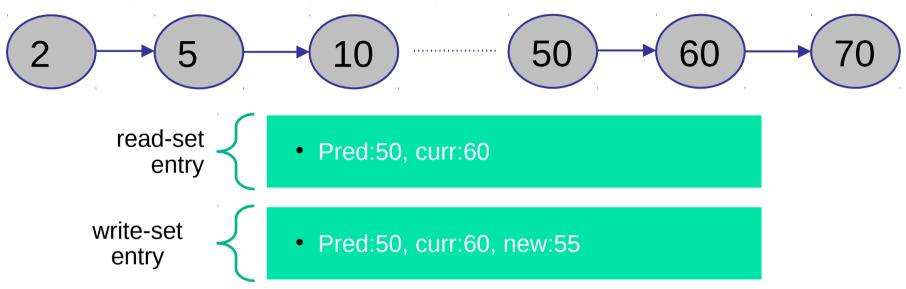
- Validation
- Commit

- Results of traversal are saved in local objects:
  - Semantic read-set: to be validated.
  - Semantic write-set: to be published at commit.

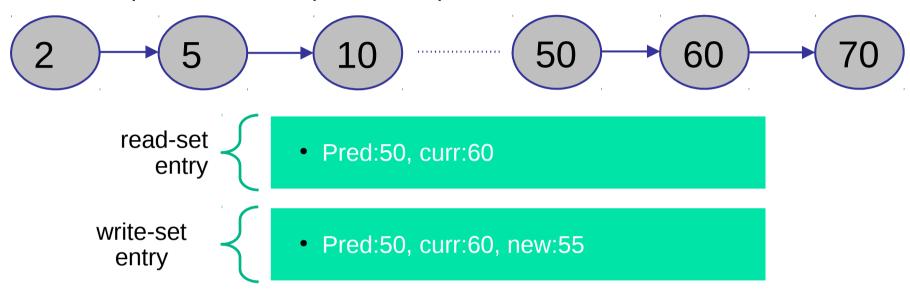
Example: Linked list (Insert "55")



Example: Linked list (Insert "55")



Example: Linked list (Insert "55")

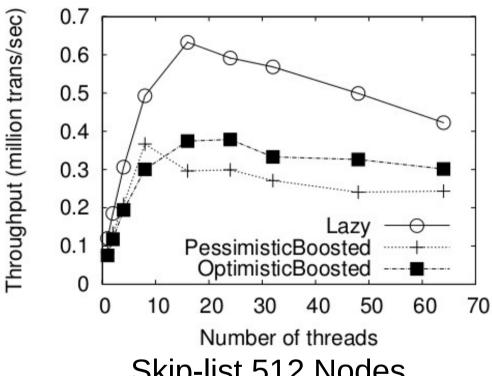


Guidelines to guarantee opacity (see OPODIS'14 paper)

### **Specific Optimizations**

- Example optimizations on Linked-List and Skip-List
  - Local elimination:
    - Ex. Add(x) then Remove(x).
    - No need to access the shared data structure.

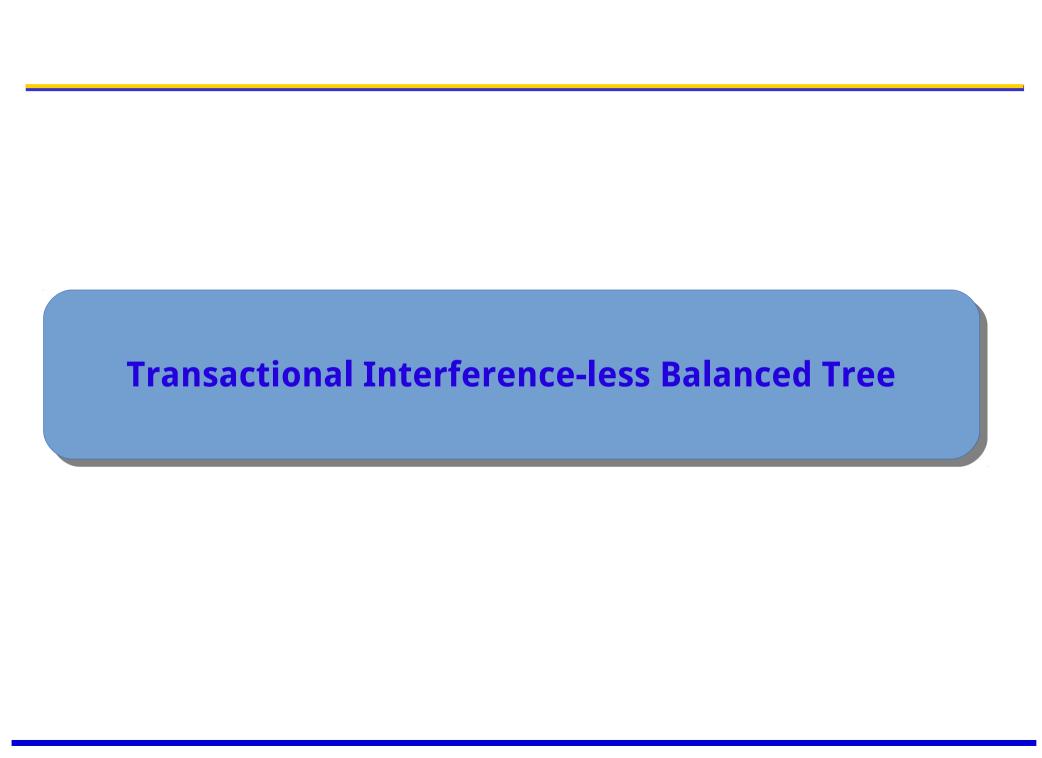
#### **Results**



1.1 Throughput (million trans/sec) 0.9 8.0 0.7 0.6 0.5 0.4 0.3 Lazv 0.2 PessimisticBoosted 0.1 OptimisticBoosted 0 40 50 70 10 20 30 60 Number of threads

Skip-list 512 Nodes 5 ops/transaction

Skip-list 64K Nodes 5 ops/transaction



#### **Transactional Interference-less Balanced Trees**

• Transactional: Functionality (following OTB's G1, G2).

• Interference-less: Performance (following OTB's G3).

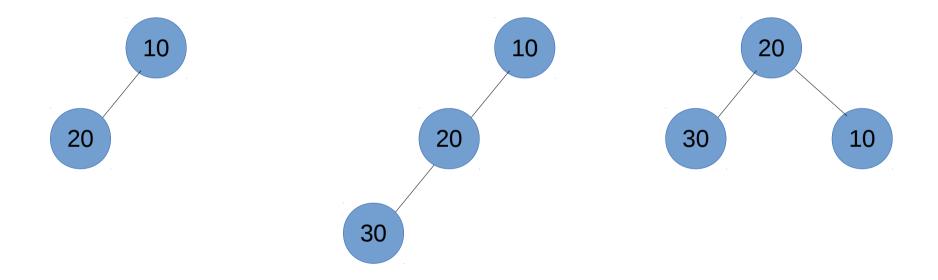
# **The Next Question**

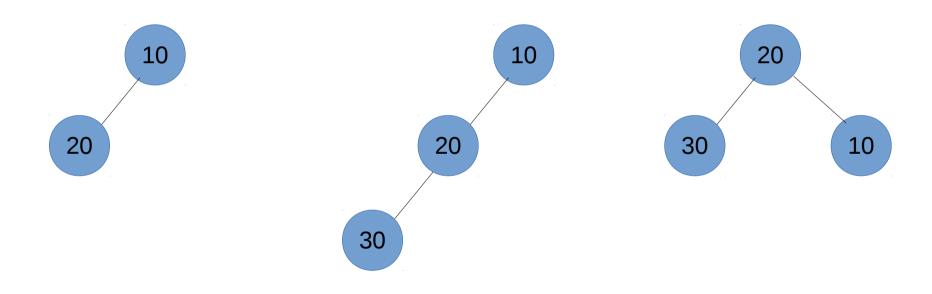
Which concurrent balanced tree design fits OTB?

# **The Next Question**

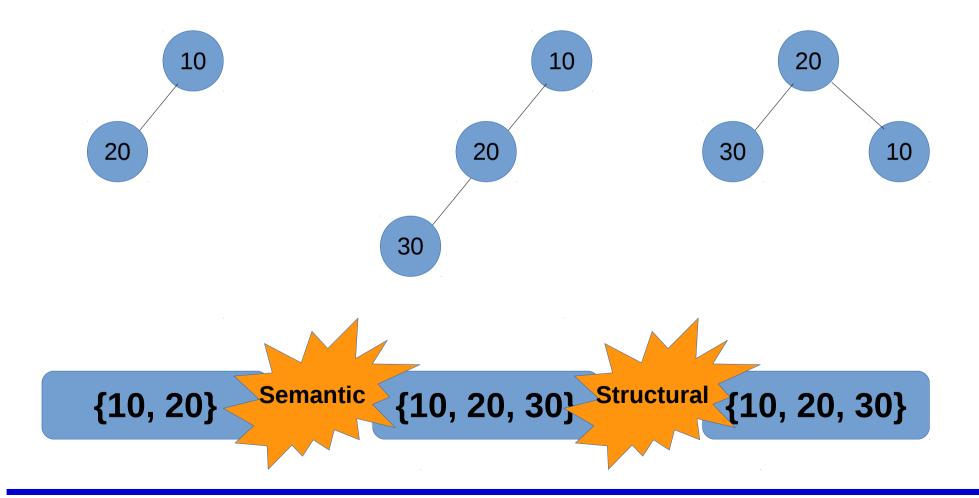
Which concurrent balanced tree design fits OTB?

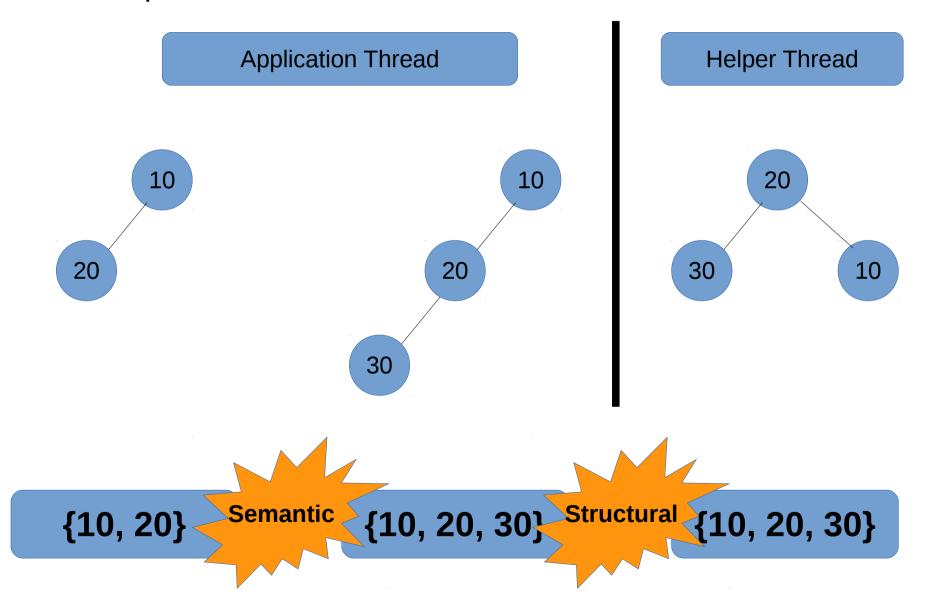
**Contention-Friendly Tree** Crain, Gramoli, & Raynal'13







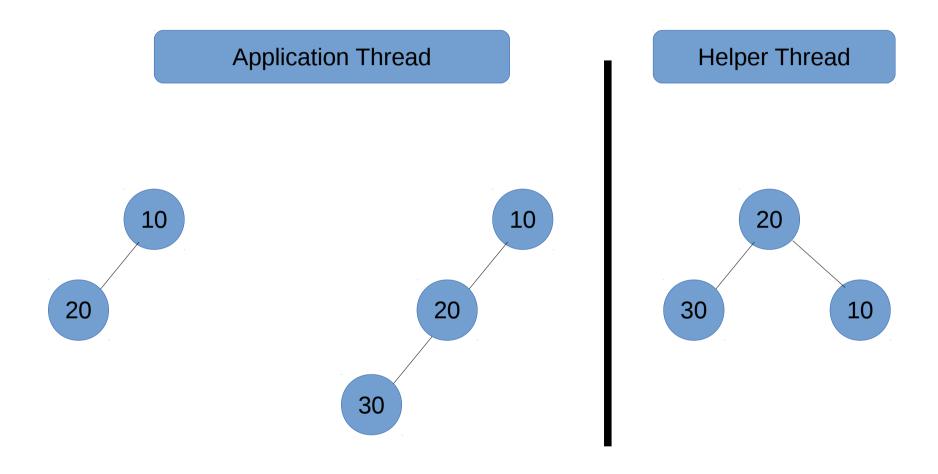




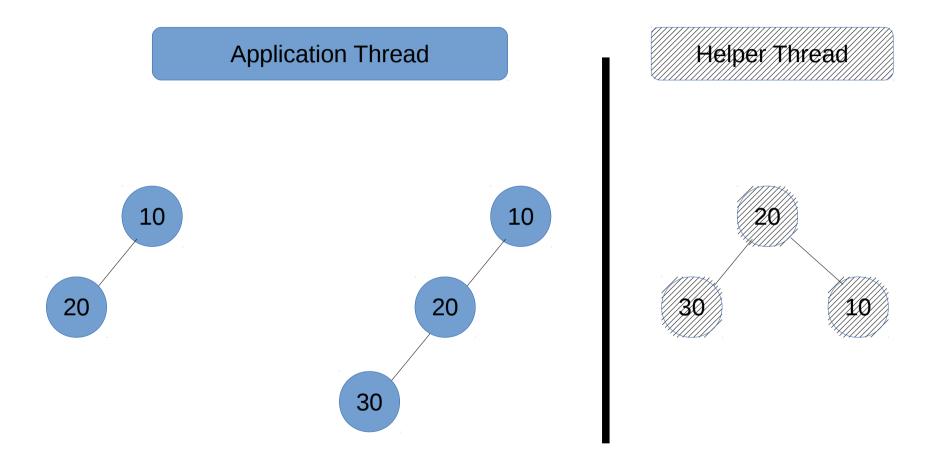
# **Our Proposal**

Transactionalizing CF-Tree using OTB (TxCF-Tree)

## **TxCF-Tree**

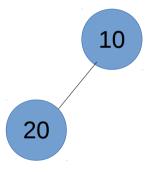


# **TxCF-Tree**



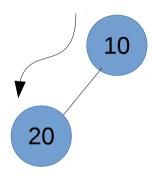
# **TxCF-Tree**

### **Application Thread**



#### **Application Thread**

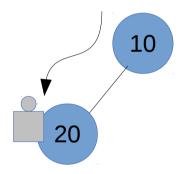
unmonitored traversal



#### **Application Thread**

unmonitored traversal

Lock & Validate

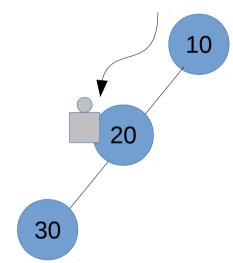


#### **Application Thread**

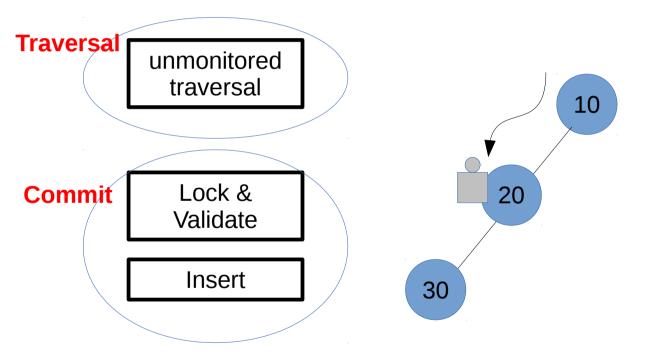
unmonitored traversal

Lock & Validate

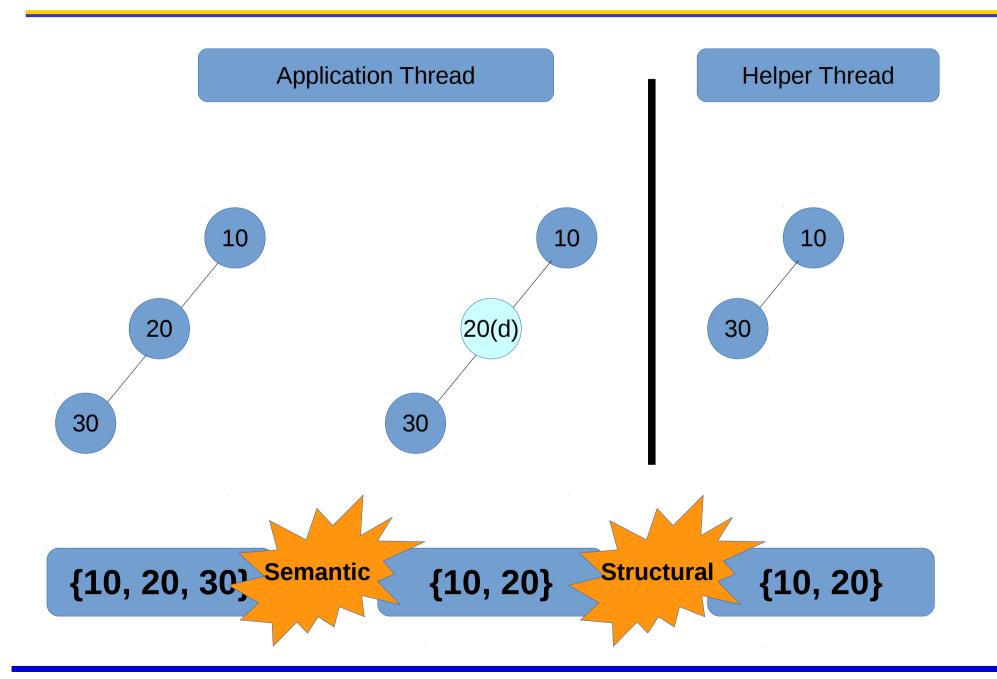
Insert



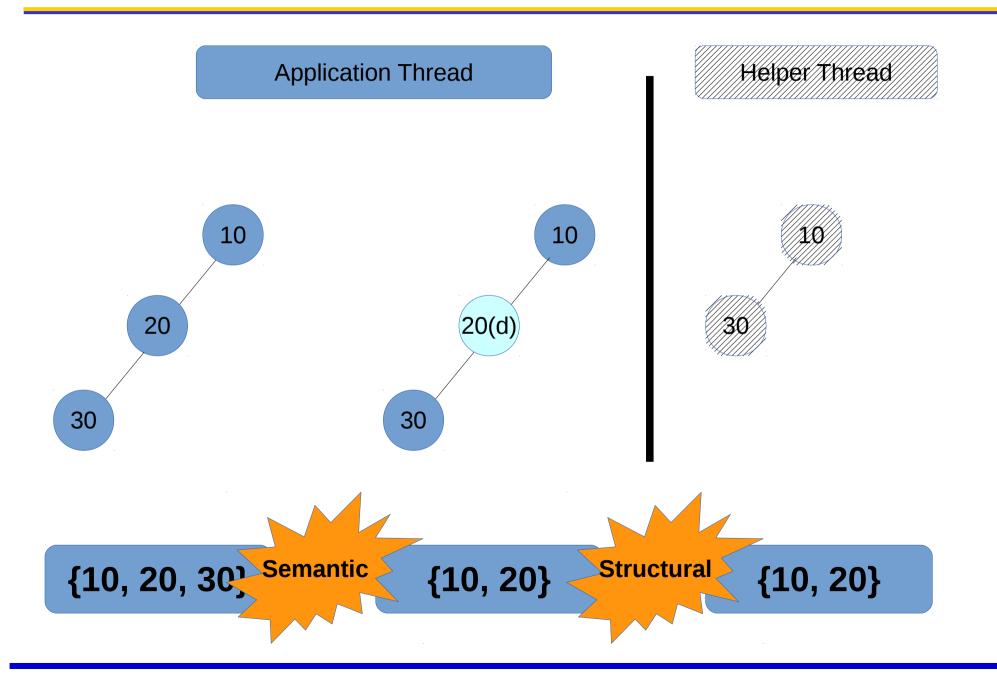
#### **Application Thread**



## Remove is similar...

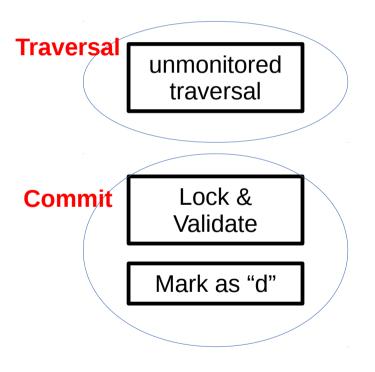


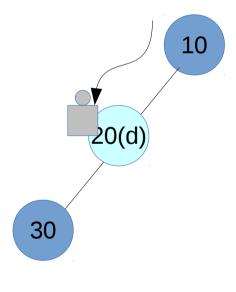
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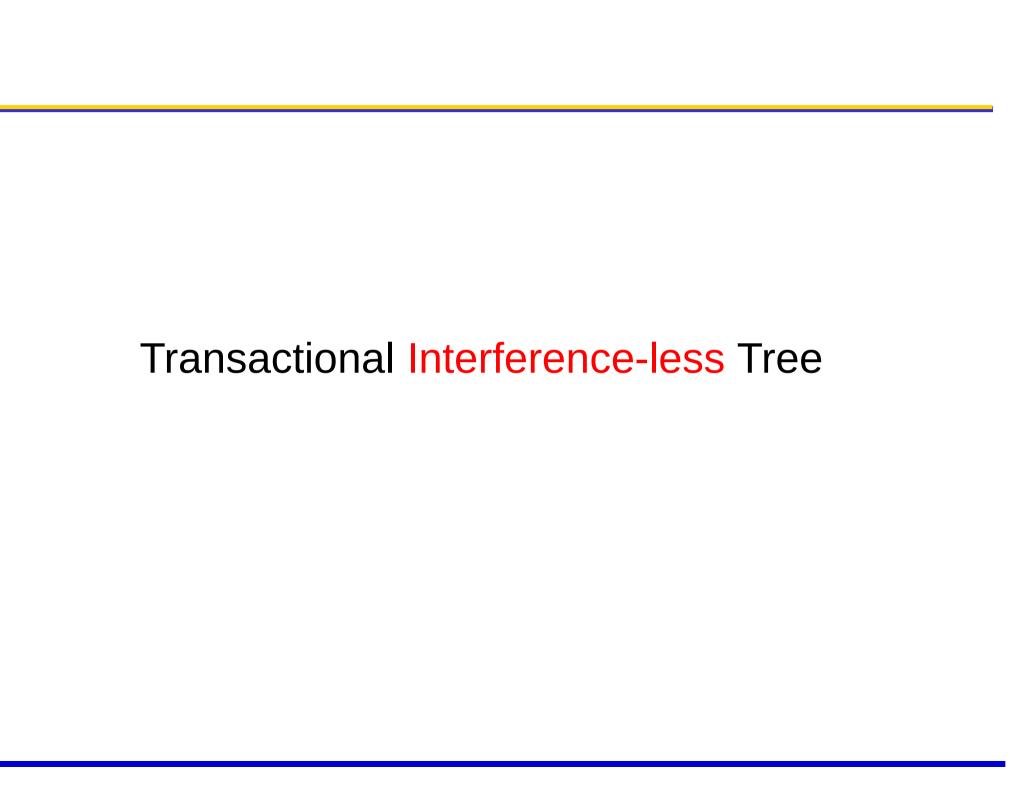


## Remove is similar...

#### **Application Thread**







## **Transactional Interference-less Tree**

- How
  - Step 1: CF-Tree!!
  - Step 2: Always give the highest priority to semantic operations over structural operations.

#### **Transactional Interference-less Tree**

#### How

- Step 1: CF-Tree!!
- Step 2: Always give the highest priority to semantic operations over structural operations.

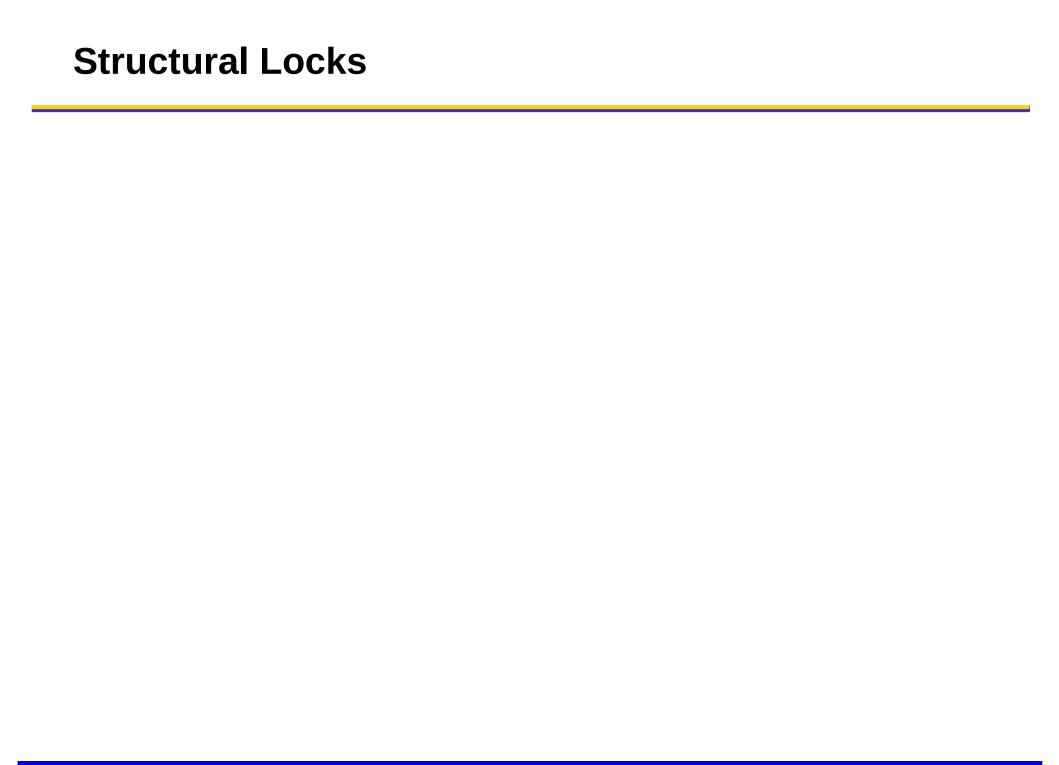
#### Why

- Aborting transactions rolls back all its operations (including the non-conflicting ones).
- Long transactions are more prone to interfere with the helper thread.

# Two building blocks

• Structural Locks.

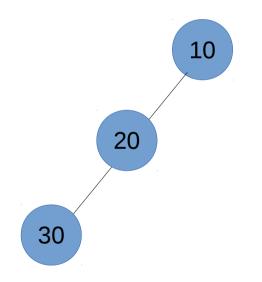
• Structural Invalidation.

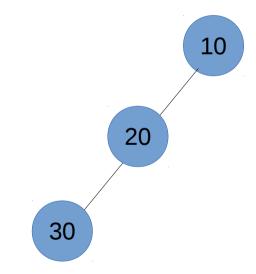


- Transaction T1 wants to delete 30.
- after traversal and before commit, assume 2 scenarios

A concurrent rotation

A concurrent delete(30)



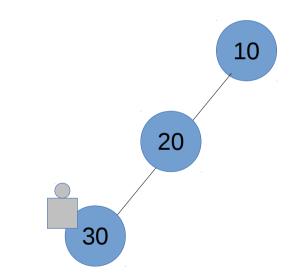


- Transaction T1 wants to delete 30.
- after traversal and before commit, assume 2 scenarios

#### A concurrent rotation

# 20

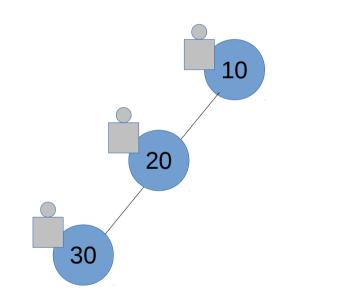
# A concurrent delete(30)

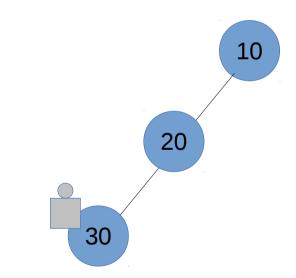


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A concurrent delete(30)

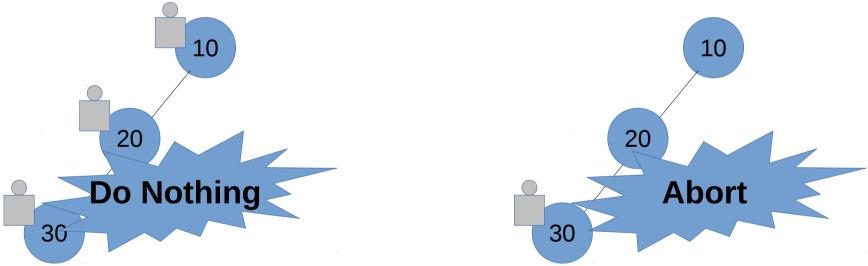




T1 observes that "30" is locked What is the best to do in both cases?

- Transaction T1 wants to delete 30.
- after traversal and before commit, assume 2 scenarios



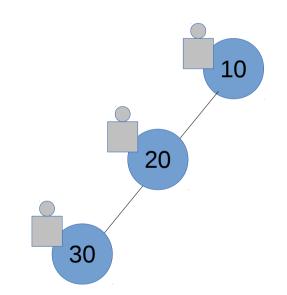


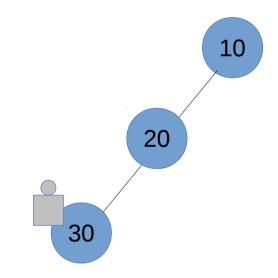
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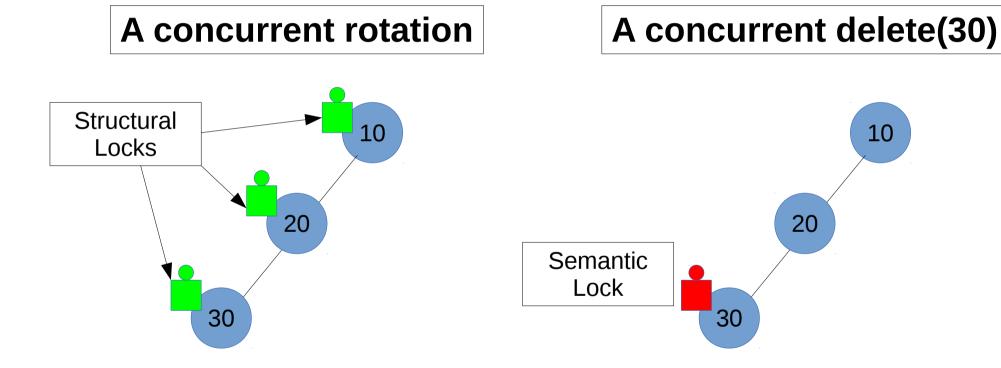
A concurrent delete(30)



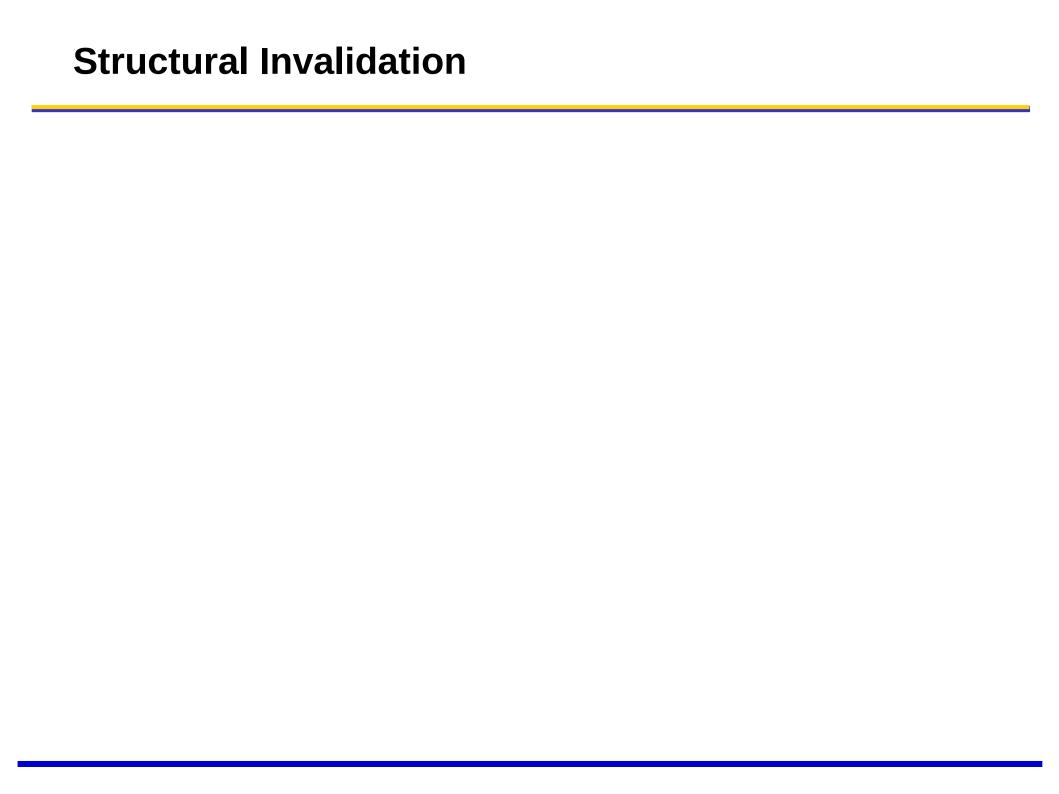


Solution?

- Transaction T1 wants to delete 30.
- after traversal and before commit, assume 2 scenarios



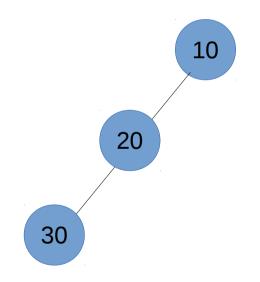
Solution?
Two types of locks

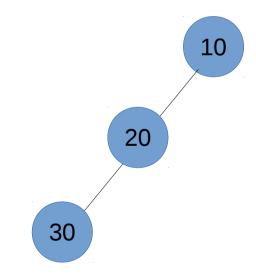


- Transaction T1 wants to insert 15.
- after traversal and before commit, assume 2 scenarios

A concurrent rotation

A concurrent insert(15)

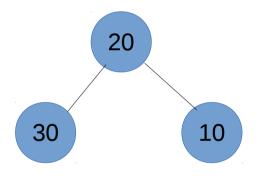


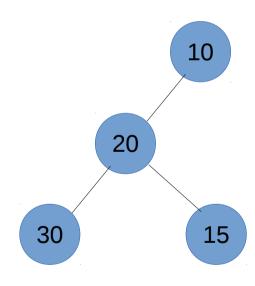


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- after traversal and before commit, assume 2 scenarios

#### A concurrent rotation

## A concurrent insert(15)

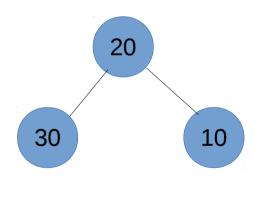


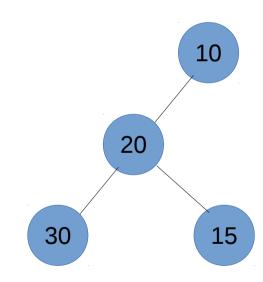


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A concurrent rotation

A concurrent insert(15)



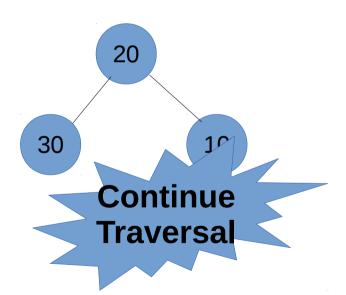


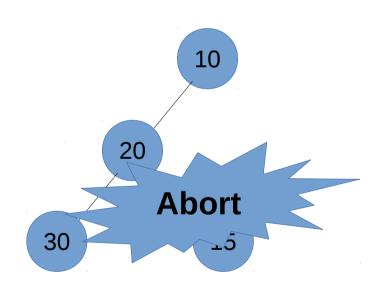
T1 observes that the right child of "20" is not NULL What is the best to do in both cases?

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A concurrent rotation

A concurrent insert(15)



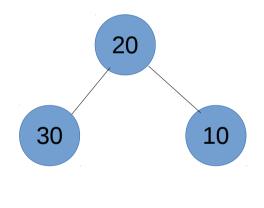


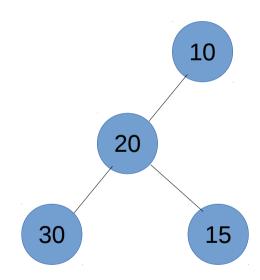
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#### A concurrent rotation

## A concurrent insert(15)



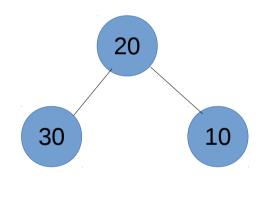


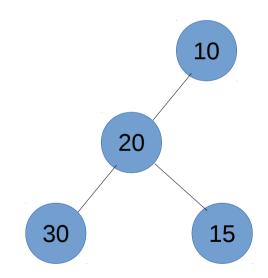
#### Solution?

- Transaction T1 wants to insert 15.
- after traversal and before commit, assume 2 scenarios

#### A concurrent rotation

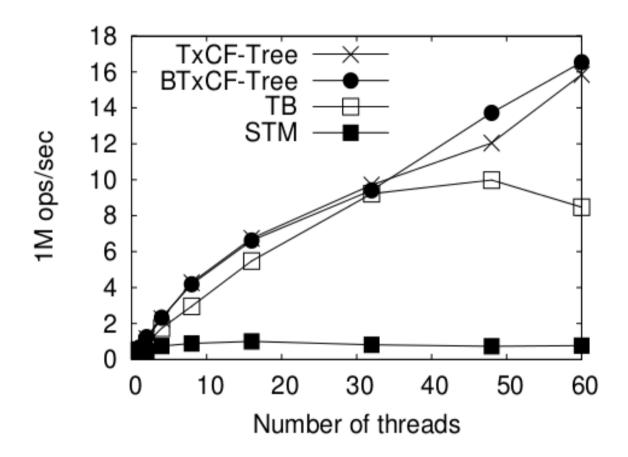
A concurrent insert(15)





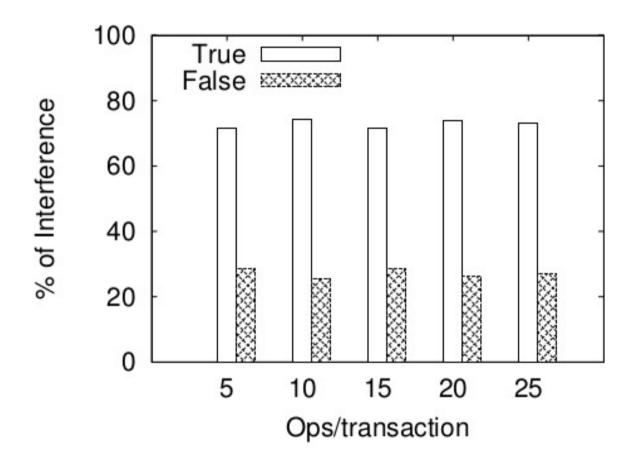
Solution?
Continue Traversal anyway

## **Evaluation**

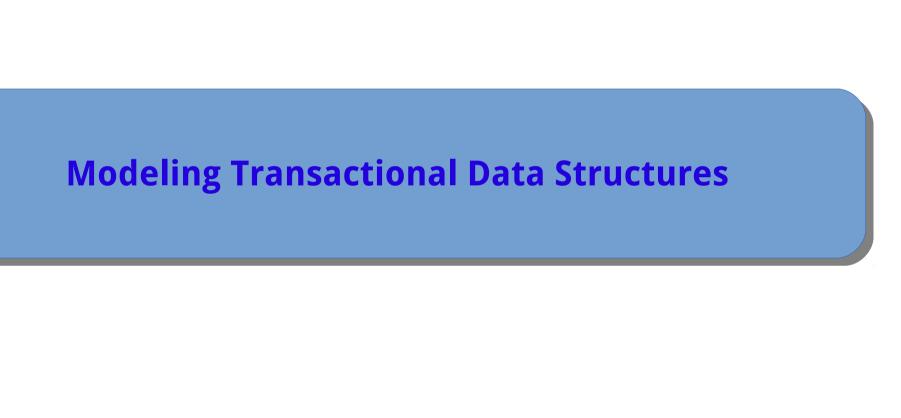


AMD 64-cores, size 10K nodes, 50% reads, 5 ops/transaction

## **Evaluation**



AMD 64-cores, size: 10K nodes, 32 threads, 50% reads, 5 ops/transaction

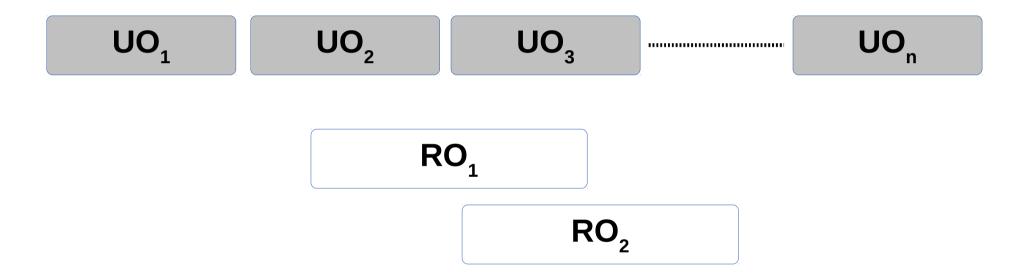


#### **Concurrent Data Structures**

- Different Designs and Implementations
  - Different ad-hoc approaches for proving correctness.

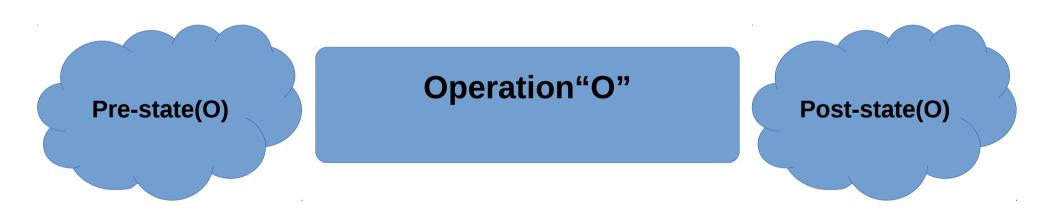
- Is there a unified model for concurrent data structures?
  - General enough.
  - Easy to use.

# SWMR Model (Lev-Ari et. Al, DISC'14)



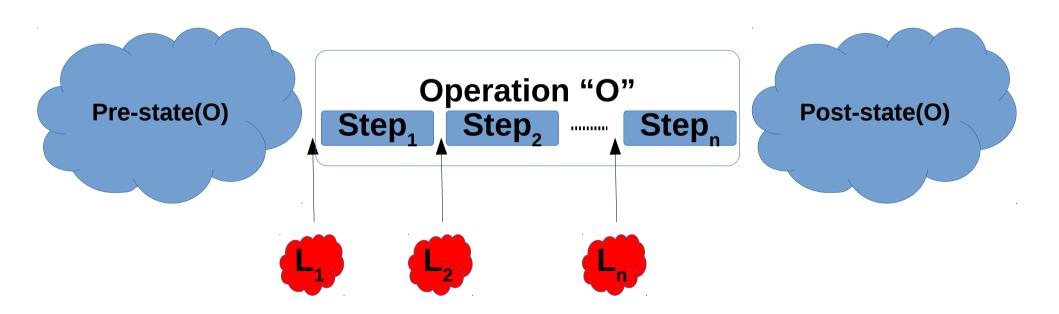
#### **Shared States**

- Data Structure is represented as a set of shared variables.
- The values of those variables is the shared state of the data structure.



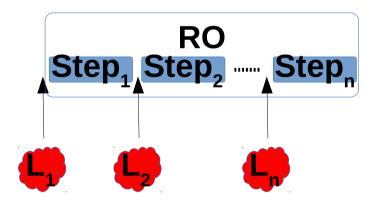
#### **Local States**

- Operation is represented as a set of steps.
- The values of the operation's local variables before any step is the local state of the step.



#### **SWMR Scenario**



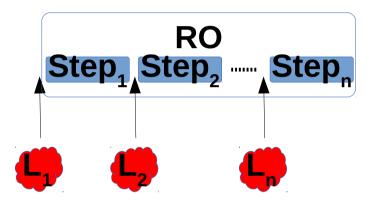


# **Validity**

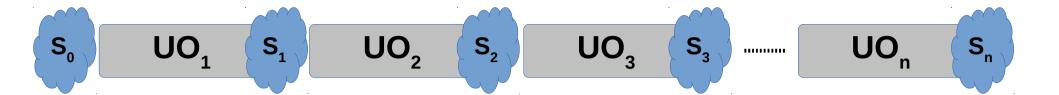


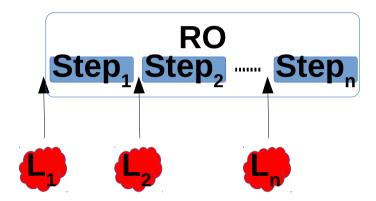
# **Validity**



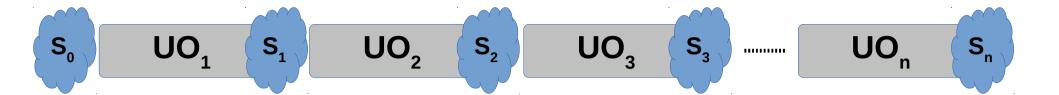


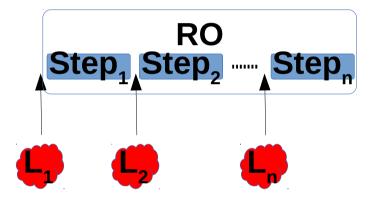
## **Validity**





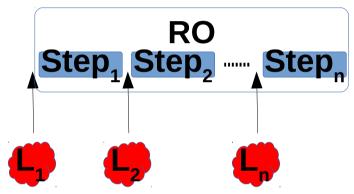
• All S<sub>i</sub> are sequentially reachable, so all UO<sub>i</sub> are valid.



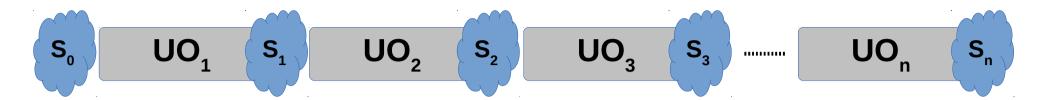


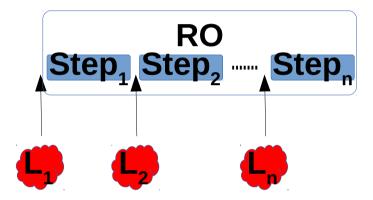
- All S<sub>i</sub> are sequentially reachable, so all UO<sub>i</sub> are valid.
- Step<sub>i</sub> in RO is valid if there is S<sub>j</sub> such that a sequential execution of RO starting from S<sub>j</sub> reaches L<sub>i</sub>.





- All S<sub>i</sub> are sequentially reachable, so all UO<sub>i</sub> are valid.
- Step<sub>j</sub> in RO is valid if there is S<sub>i</sub> such that a sequential execution of RO starting from S<sub>i</sub> reaches L<sub>j</sub>.





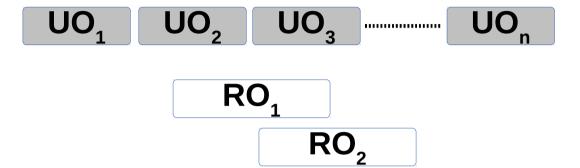
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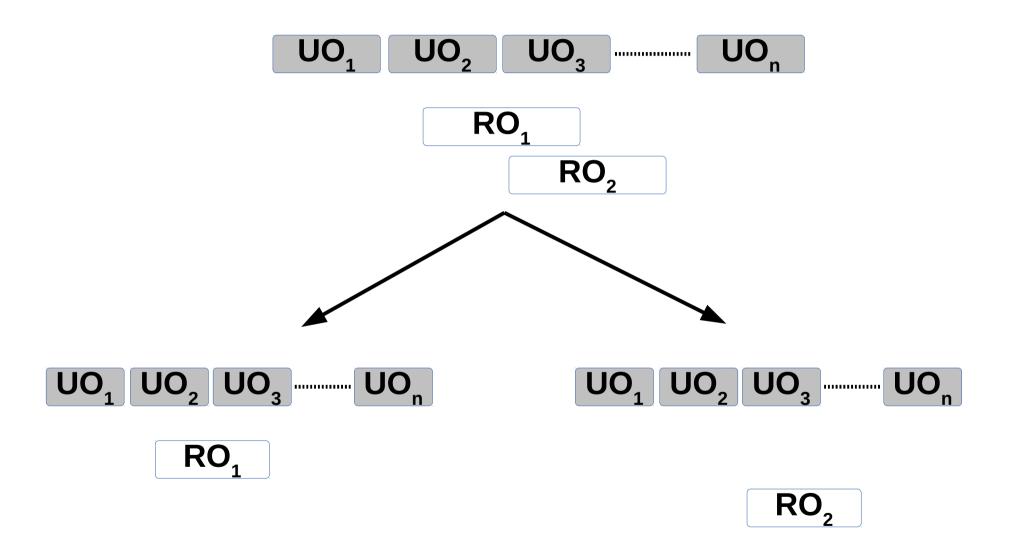
 Step<sub>j</sub> in RO is valid if there is a "base point" where the "base condition" of step<sub>j</sub> holds.

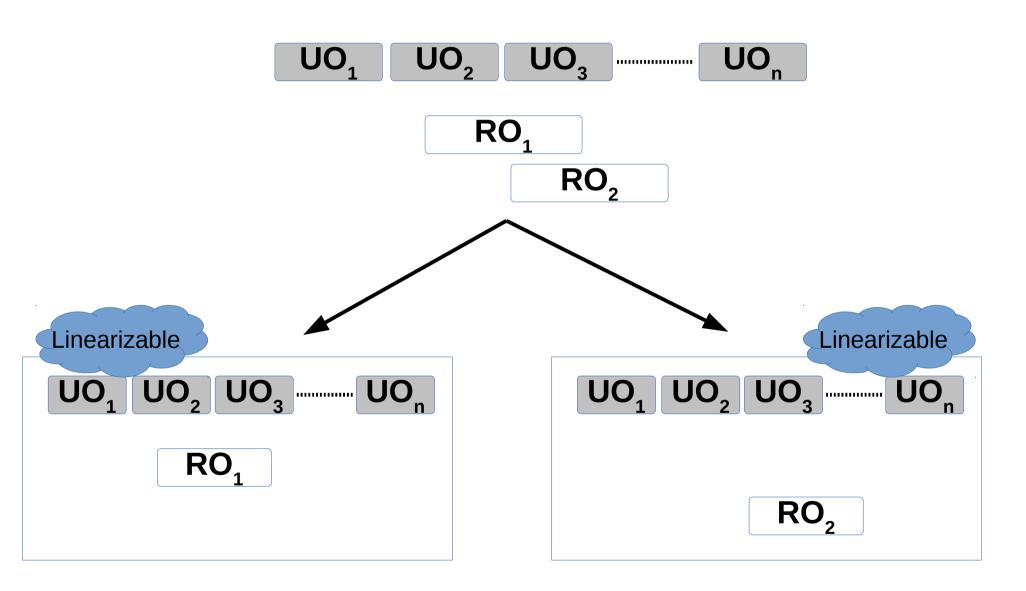
- How to prove validity for any data structure.
  - Identify the base conditions for each step in each operation (it is sufficient to do so only for steps that access the shared memory).
  - Prove that in any concurrent execution, every step has a base point that satisfies its base condition.

- How to prove validity for any data structure.
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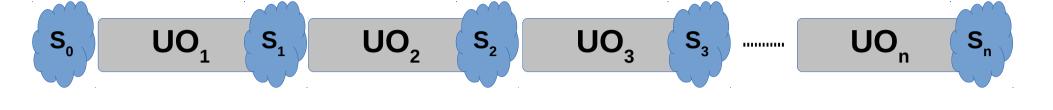


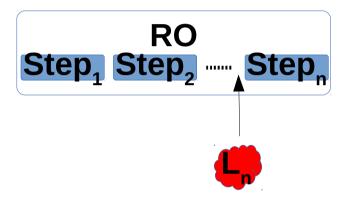






RO Step<sub>1</sub> Step<sub>2</sub> Step<sub>n</sub>





- Acceptable base points for RO's return step are only S<sub>1</sub>, S<sub>2</sub>, S<sub>3</sub>.
  - Observes either the last update or a concurrent update.

```
Function remove(n)
p \leftarrow \bot
next \leftarrow read(head.next)
while next \neq n
p \leftarrow next
next \leftarrow read(p.next)
write(p.next, n.next)

Function insertLast(n)
last \leftarrow readLast()
write(last.next, n)
```

```
Base conditions: Function readLast()
n \leftarrow \bot
\Phi_1 : true
next \leftarrow read(head.next)
while next \neq \bot
n \leftarrow next
p_2 : head \stackrel{*}{\Rightarrow} n
p_3 : head \stackrel{*}{\Rightarrow} n
next \leftarrow read(n.next)
next \leftarrow read(n.next)
next \leftarrow read(n.next)
next \leftarrow read(n.next)
```

```
Function remove(n)
p \leftarrow \bot
next \leftarrow read(head.next)
while next \neq n
p \leftarrow next
next \leftarrow read(p.next)
write(p.next, n next)
```

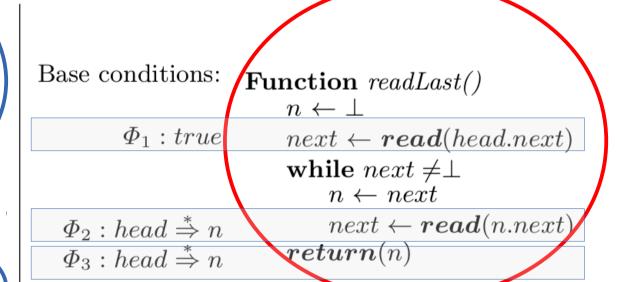
Function insertLast(n)  $last \leftarrow readLast()$ write(last.next, n) Base conditions:

 $\Phi_1: true$ 

 $\Phi_2 : head \stackrel{*}{\Rightarrow} n$  $\Phi_3 : head \stackrel{*}{\Rightarrow} n$  Function readLast()  $n \leftarrow \bot$   $next \leftarrow read(head.next)$ while  $next \neq \bot$   $n \leftarrow next$   $next \leftarrow read(n.next)$  return(n)

```
Function remove(n)
p \leftarrow \bot
next \leftarrow read(head.next)
while next \neq n
p \leftarrow next
next \leftarrow read(p.next)
write(p.next, p.next)
```

Function insertLast(n)  $last \leftarrow readLast()$ write(last.next, n)



# Where is the Problem? It covers only single-writer designs It does not cover composable designs

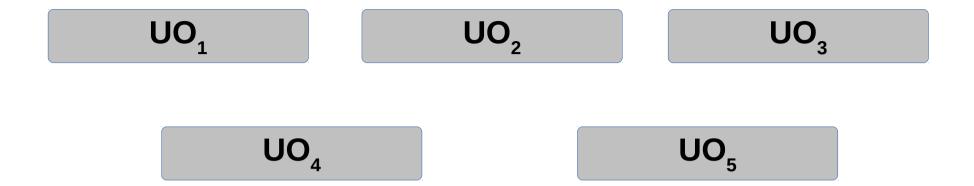
Can we cover a wider set?

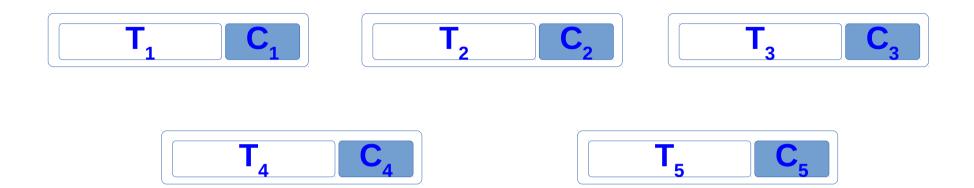
Optimistic Composable Data Structures

#### **Our Models**

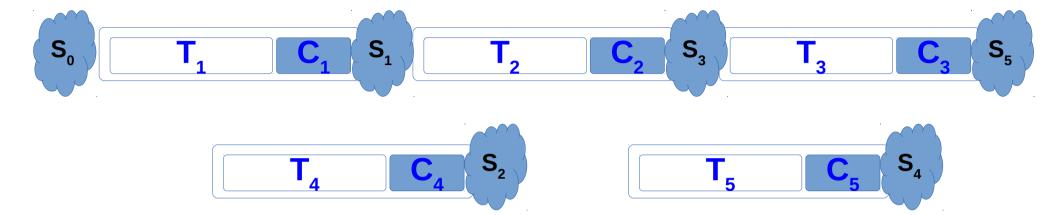
Single Writer Commit (SWC)

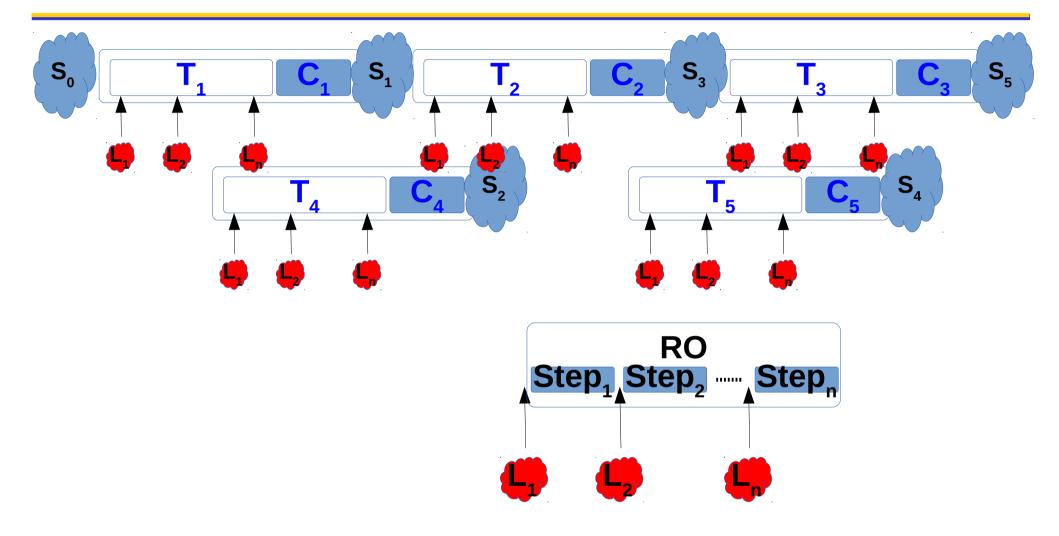
Composable SWC (C-SWC)











#### **Even More...**

- Do we really need single commit at a time:
  - NO!!!
  - It is enough to execute commit phases atomically with single lock atomicity (SLA) guarantees.
  - More practical alternatives:
    - HTM (e.g. Intel TSX).
    - STM (e.g. NOrec "the SLA version").

```
1: procedure READLAST
 2:
            last \leftarrow 1
            next \leftarrow \mathbf{read}(head.next)
                                                                                             \triangleright \phi_1 : true
 4:
            while next \neq \perp do
 5:
                 last \leftarrow next
 6:
                                                                                \triangleright \phi_2 : head \stackrel{*}{\Rightarrow} last
                 next \leftarrow \mathbf{read}(last.next)
                                                                                \triangleright \phi_3 : head \stackrel{*}{\Rightarrow} last
 7:
            return(last)
 8: end procedure
 9: procedure INSERTLAST(n)
10:
            last \leftarrow \bot
11:
            next \leftarrow \mathbf{read}(head.next)
                                                                                             \triangleright \phi_4 : true
12:
            while next \neq \perp do
13:
                 last \leftarrow next
                                                                                \triangleright \phi_5 : head \stackrel{*}{\Rightarrow} last
14:
                 next \leftarrow \mathbf{read}(last.next)
15:
            lockAcquire(gl)
                                                                                \triangleright \phi_6 : head \stackrel{*}{\Rightarrow} last
16:
            if read(last.next) \neq \perp then
17:
                 lockRelease(gl)
18:
                 go to 10
19:
            write(last.next, n)
20:
            lockRelease(gl)
21: end procedure
```

```
procedure READLAST
            last \leftarrow \perp
            next \leftarrow \mathbf{read}(head.next)
                                                                                               \triangleright \phi_1 : true
            while next \neq \perp do
                  last \leftarrow next
 6:
                                                                                  \triangleright \phi_2 : head \stackrel{*}{\Rightarrow} last
                  next \leftarrow \mathbf{read}(last.next)
                                                                                  \triangleright \phi_3 : head \stackrel{*}{\Rightarrow} last
            return(last)
  8: end procedure
 9: procedure INSERTLAST(n)
            last \leftarrow \perp
11:
            next \leftarrow \mathbf{read}(head.next)
                                                                                               \triangleright \phi_4 : true
12:
            while next \neq \perp do
13:
                  last \leftarrow next
                                                                                  \triangleright \phi_5 : head \stackrel{*}{\Rightarrow} last
                  next \leftarrow \mathbf{read}(last.next)
            lockAcquire(gl)
                                                                                   \triangleright \phi_6 : head \stackrel{*}{\Rightarrow} last
16:
            if read(last.next) \neq \perp then
17:
                  lockRelease(gl)
18:
                  go to 10
19:
            write(last.next, n)
20:
            lockRelease(gl)
21: end procedure
```

```
procedure READLAST
          last \leftarrow \perp
          next \leftarrow \mathbf{read}(head.next)
          while next \neq \perp do
              last \leftarrow next
 6:
              next \leftarrow \mathbf{read}(last.next)
          return(last)
 8: end procedure
 9: procedure INSERTLAST(n)
          last \leftarrow \perp
11:
          next \leftarrow \mathbf{read}(head.next)
12:
          while next \neq \perp do
13:
              last \leftarrow next
              next \leftarrow \mathbf{read}(last.next)
          lockAcquire(gl)
16:
          if read(last.next) \neq \perp then
17:
              lockRelease(gl)
18:
              go to 10
19:
          write(last.next, n)
20:
          lockRelease(gl)
21: end procedure
```

```
\triangleright \phi_1 : true
\triangleright \phi_2 : head \stackrel{*}{\Rightarrow} last
\triangleright \phi_3 : head \stackrel{*}{\Rightarrow} last
                        \triangleright \phi_4 : true
\triangleright \phi_5 : head \stackrel{*}{\Rightarrow} last
 \triangleright \phi_6 : head \stackrel{*}{\Rightarrow} last
```

#### Composable SWC Model (C-SWC)

```
1: procedure ATOMIC:T_1

2: x = 5

3: if readLast() \neq x then

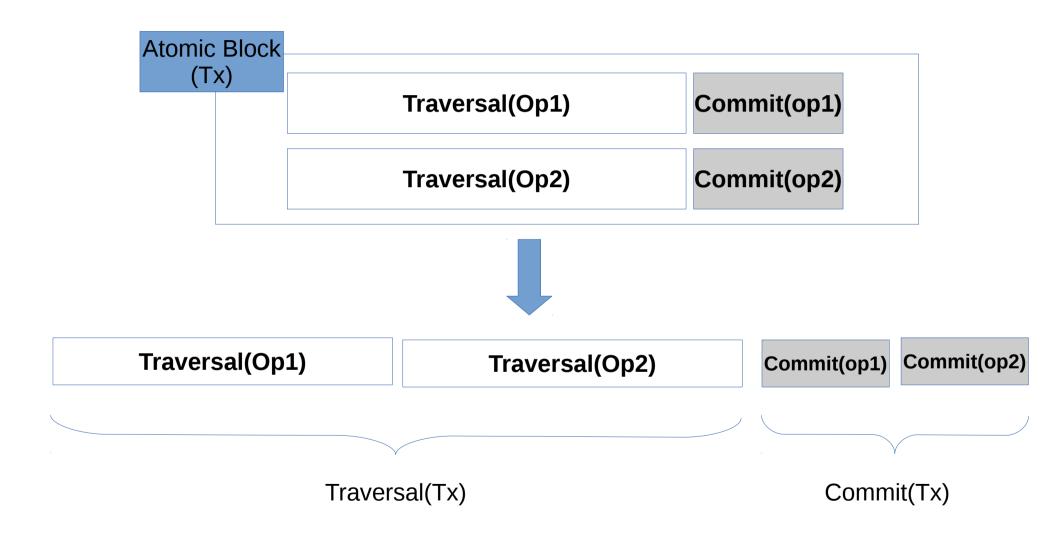
4: insertLast(x)

5: if readLast() \neq x then

6: ... // illegal execution
```

7: end procedure

#### Composable SWC Model (C-SWC)



#### What is remaining?

- Internal Consistency.
  - The commit phase of each operation reflects what the operation observed in its traversal.
  - The shared state of an operation is visible to subsequent operations in the same transaction.

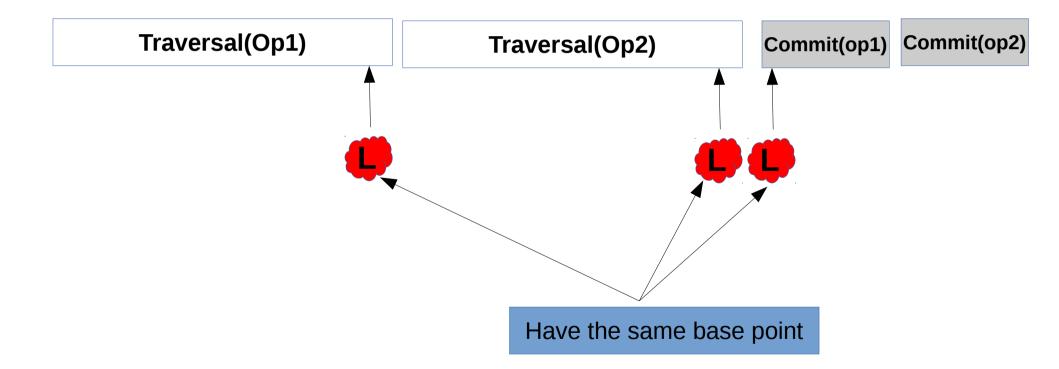
### How to prove internal consistency?

Traversal(Op1)

Traversal(Op2)

Commit(op1) Commit(op2)

#### How to prove internal consistency?



# Conclusions

#### **Our Contributions**

#### Composability

Optimistic Transactional Boosting PPoPP 2014

OTB-Set OPODIS 2014

TxCF-Tree DISC 2015

Transactional Data Structures

#### Integration

Integration with STM TRANSACT 2014

Integration with HTM Under submission

Remote Transaction Commit IEEE TC 2015

Remote Invalidation IPDPS 2014

Modeling

SWC and C-SWC Models WTTM 2015, under submission

# Questions?